



1. In the circuit of Fig. 1, find the values of  $V_{ab}$  and  $V_{cd}$ . (10%). (10%)
2. In the circuit of Fig. 2, find the value of  $V_o$  using the mesh current method. (20%)

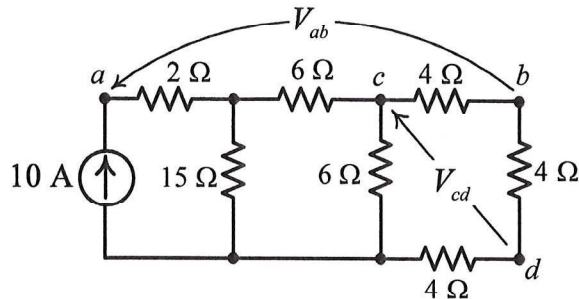


Fig. 1

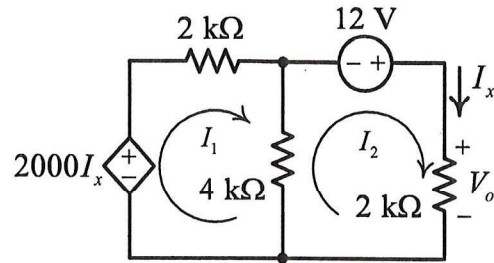


Fig. 2

3. Referring to Fig. 3, the switch closes at  $t=0$ , and the initial conditions are  $i(0)=0$  and  $v(0)=0$ .
  - (a) Calculate the final conditions  $v(\infty)$  and  $i(\infty)$ . (6%)
  - (b) Find the circuit's natural frequencies  $s_1$  and  $s_2$ . (6%)
  - (c) Calculate the capacitor's voltage  $v(t)$  for  $t > 0$ . (8%)
4. Find the current  $I$  in the circuit in Fig. 4. (16%)

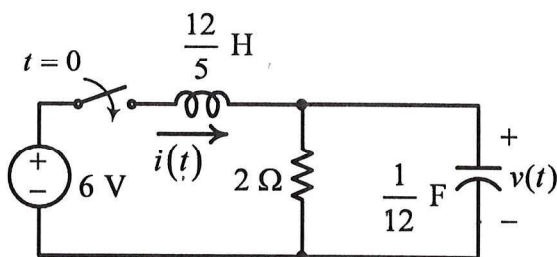


Fig. 3

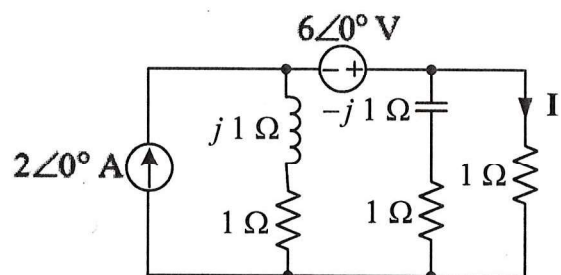


Fig. 4

5. Find the current  $I_1$  and the output voltage  $V_o$  in the circuit in Fig. 5. (16%)
6. In the balanced three-phase system shown in Fig. 6, the line voltage is 34.5 kV rms at 60 Hz. Find the values of the capacitors  $C$  such that the total load has a power factor of 0.90 lagging. (18%)

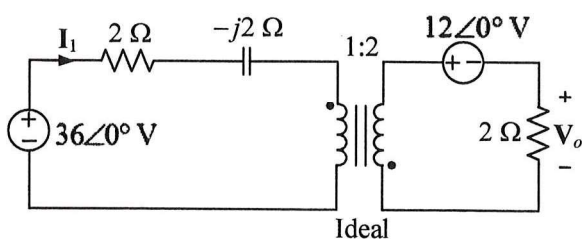


Fig. 5

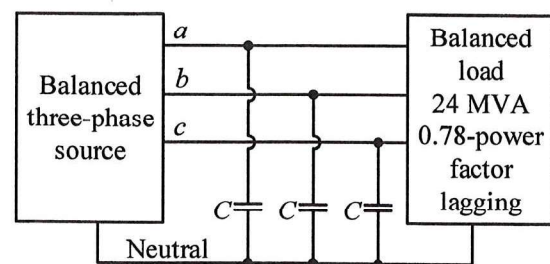


Fig. 6



1. (15%) Solve the general solution of the following differential equations:
  - (1)  $\frac{dy}{dx} = e^{2x-3y}$  (5%)
  - (2)  $x \frac{dy}{dx} - y = x^2 \sin x$  (5%)
  - (3)  $y^3 dx + 3xy^2 dy = 0$  (5%)
2. (10%) Solve the initial value problem:  $5y'' + y' = -6x$ ,  $y(0) = 0$ ,  $y'(0) = -10$
3. (15%) Find the given Laplace transform or inverse transform:
  - (1)  $\mathcal{L}\{e^t(\cos \omega t - 2\sin \omega t)\}$  (5%)
  - (2)  $\mathcal{L}^{-1}\left\{\frac{3}{s(s^2+9)}\right\}$  (5%)
  - (3)  $\mathcal{L}\left\{\int_0^t \tau e^{t-\tau} d\tau\right\}$  (5%)
4. (10%) Find the Fourier series of  $f(t) = \pi + t$  on the interval  $-\pi < t < \pi$ .
5. (10%) Find parameter equation of line L through the point  $P_0(2, 3, -4)$  and  $P_1(3, -2, 5)$ .
6. (20%) Let  $V$  be  $R^3$  and let  $S = \{\mathbf{v}_1, \mathbf{v}_2, \mathbf{v}_3\}$  and  $T = \{\mathbf{w}_1, \mathbf{w}_2, \mathbf{w}_3\}$  be ordered bases for  $R^3$ .
 
$$\mathbf{v}_1 = [2 \ 0 \ 1]^T, \mathbf{v}_2 = [1 \ 2 \ 0]^T, \mathbf{v}_3 = [1 \ 1 \ 1]^T,$$

$$\mathbf{w}_1 = [6 \ 3 \ 3]^T, \mathbf{w}_2 = [4 \ -1 \ 3]^T, \mathbf{w}_3 = [5 \ 5 \ 2]^T,$$
  - (1) Compute the transition matrix  $P_{S \leftarrow T}$  from the T-basis to the S-basis. (10%)
  - (2) This is the vector  $\mathbf{v} = [4 \ -9 \ 5]^T$ . Express the  $\mathbf{v}$  in terms of S-basis and T-basis. (10%)
7. (20%) Let the matrix  $A$  is a symmetric matrix.

$$A = \begin{bmatrix} 0 & 2 & 2 \\ 2 & 0 & 2 \\ 2 & 2 & 0 \end{bmatrix}$$

Find the orthogonal matrix  $P$  such that  $P^{-1}AP = P^TAP = D$ .  $D$  is a diagonal matrix. The eigenvalues of  $A$  lie on the main diagonal of  $D$ .