



1. (15%) A differential equation is as follows,

$$x^3y^4 + (x^4y^3 + 2y)\frac{dy}{dx} = 0$$

- (a) Find its solution.
 (b) Verify your solution in (a).
2. (15%) A 2nd-order differential equation is as follows,

$$y'' + 9y' + 20y = -36e^{-t}, y(0) = 0, y'(0) = 0$$

- (a) (05%) Find the general solution of the homogeneous equation.
 (b) (05%) Find a particular solution of the non-homogeneous equation.
 (c) (05%) Find the final particular solution of this non-homogeneous equation.
3. (20%) A differential equation system is as follows,

$$y' = \begin{bmatrix} 2 & -2 \\ -1 & 3 \end{bmatrix} y + \begin{bmatrix} 4 \\ 2 \end{bmatrix} e^{2t}, y(0) = 0$$

- (a) (05%) Find the Laplace transform of e^{2t} .
 (b) (10%) Find the solution of this differential equation system using Laplace transform.
 (c) (05%) Determine the stability of this system and explain your reason.
4. (15%) Perform the indicated operation, give that:

$$A = \begin{bmatrix} 1 & 0 & -1 \\ 2 & 1 & 3 \end{bmatrix} \quad B = \begin{bmatrix} 2 & 1 & 0 \\ 0 & 3 & 4 \end{bmatrix} \quad C = \begin{bmatrix} -1 & 2 \\ 3 & 4 \\ 0 & 1 \end{bmatrix} \quad D = \begin{bmatrix} 0 & 1 \\ -1 & 0 \\ 2 & 1 \end{bmatrix}$$

- (a) $(A+B)^T$ (b) $(2A-B)(C+D)$ (c) If $2X+3(A-B)=0$, Find X
5. (10%) Solve the system using either Gaussian elimination with back-substitution.

$$0x + 4y - 2z = 2$$

$$6x - 2y + z = 29$$

$$4x + 8y - 4z = 24$$

6. (15%) If $\vec{A} = \vec{i} - 3\vec{j} + 2\vec{k}$, $\vec{B} = 3\vec{i} - 2\vec{j} + 3\vec{k}$, Find (a) $\vec{A} \cdot \vec{B}$ (b) $\vec{A} \times \vec{B}$ (c) The projection of \vec{A} on \vec{B}
7. (10%) Find the eigenvalues and eigenvectors of A.

$$A = \begin{bmatrix} 2 & 0 & 1 \\ 0 & 1 & 0 \\ 2 & 0 & 3 \end{bmatrix}$$



$h = 6.63 \times 10^{-34}$ J-s, $k = 8.62 \times 10^{-5}$ eV/K, $q = 1.6 \times 10^{-19}$ C, $\ln 10 \approx 2.3$, $\epsilon_{\text{Si}} = 12 \times 8.85 \times 10^{-14}$ F/cm, $n_i = 10^{10}$ cm⁻³

1. Explain the following terms: (a) Lattice vibration (b) Vacancy (10%)
2. What kind of impurity atom can be added to make the following intrinsic materials to become *n*-type semiconductors? (a) Si (b) GaAs (10%)
3. GaAs is more suited than Si for use in optical devices. Please explain why. (10%)
4. Consider the Fermi-Dirac probability function $f_F(E)$, and E_F is the Fermi energy. Assume there are two temperatures $T_1 = 0$ K and $T_2 > 0$ K.
 - (a) Plot the curve of $f_F(E)$ vs. E for T_1 . (5%)
 - (b) Plot the curve of $f_F(E)$ vs. E for T_2 . (5%)
5. The Hall effect can be used to distinguish whether a semiconductor is *n*-type or *p*-type. Please describe its principle. (10%)
6. Explain or define the following terms:
 - (a) Miller indices (5%)
 - (b) Low injection level (5%)
 - (c) Strong inversion condition of MOS structure (5%)
7. Explain the dominant current is electron or hole current of p^+n , n^+p , Np and Pn junctions, where N and P mean wider energy gap and $+$ means high doping concentration. (15%)
8. A silicon *pin* junction has the doping profile shown in Fig. 1. The “*i*” corresponds to an ideal intrinsic region in which there is no impurity doping concentration. A reverse-bias voltage is applied to the *pin* junction so that the total depletion width extends from -1.5 μm to $+1.5$ μm as shown in follow. (a) Calculate the magnitude of the electric field at $x = 0$. (b) Sketch the electric field through the *pin* junction. (c) Calculate the reverse bias that must be applied. (20%)

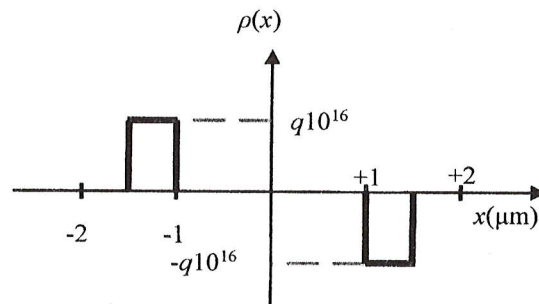


Fig. 1



1. () In C language, the semicolon (;) is used to mark the (A)start (B)end (C)separator (D)nothing of a statement. (10 pts)
2. () What type of loop always executes at least once? (A)for (B)while (C)switch/case (D) do/while. (10 pts)
3. () What is the value of sum after the following code has executed? (A)55 (B)45 (C) 10 (D) none of these. (10 pts)

```
for(sum=0,i=1;i<=10;i++) sum+=i;
```

4. () How to do an infinite loop? (A) int n=1; while(n!= 0) ++n; (B)while('indefinite'); (C) while(1); (D) while(0). (10 pts)

5. Change this program so that it uses “switch...case” command instead of “if-else”. (10 pts)

```
if (month == 4 || month == 6 || month == 9 || month == 11)
```

```
    printf("Month has 30 days.\n");
```

```
else if (month == 1 || month == 3 || month == 5 || month == 7 || month == 8 || month == 10 || month == 12)
```

```
    printf("Month has 31 days.\n");
```

```
else if (month == 2)
```

```
    printf("Month has 28 or 29 days.\n");
```

```
else
```

```
    printf("Don't know that month.\n");
```

6. Write a program to do bubble sort to sort n numbers in an array Arr. You can use any programming language or pseudo language. What is the time complexity of bubble sort? (12.5 pts)
7. Write a program to do matrix multiplication for a r1*c1 matrix and a c1*c2 matrix, resulting in a r1*c2 matrix. What is the time complexity of your algorithm? (12.5 pts)
8. Write a program to find the index of a number X in a sorted array of length n. What is the time complexity of your algorithm? (12.5 pts)
9. Write a program to find the greatest common divisor of two positive integers a and b. (12.5 pts)



本試題共五題，每題得分如各題中所示，共計 100 分，請依題號作答並將答案寫在答案卷上，違者不予計分。

1. (10 分) As shown in Fig. P1, a first-order low-pass active filter performs a low-pass STC function. Derive the transfer function and show the DC gain is $(-R_2/R_1)$ and the 3 dB frequency $\omega_o = 1/CR_2$.

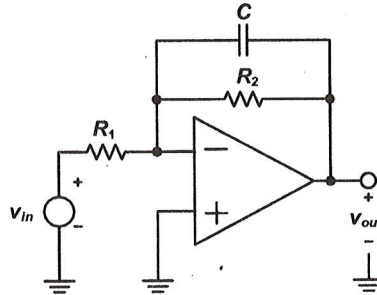


Fig. P1

2. In the capacitor coupled attenuator circuit shown in Fig P2, I is a DC current that varies from 0 mA to 1 mA, D_1 and D_2 are diodes with $n = 1$, and C_1 and C_2 are large coupling capacitors. For very small input signals,
- (10 分) find the value of the ratio v_{out} / v_{in} for I equal to 10 μA .
 - (5 分) find the value of the ratio v_{out} / v_{in} for I equal to 100 μA .
 - (5 分) find the value of the ratio v_{out} / v_{in} for I equal to 500 μA .

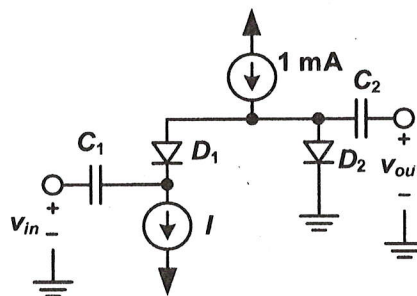


Fig. P2

3. As Fig. P3 shows, using $V_{DD} = 6 \text{ V}$ with an NMOS for which $V_t = 1.2 \text{ V}$, $k_n' W/L = 2.0 \text{ mA/V}^2$ and $\lambda = 0$, provide a design which biases the transistor at $I_D = 2 \text{ mA}$, with V_{DS} large enough to allow saturation operation for a 2 V negative signal swing at the drain. Use a 26 M Ω resistor as the R_{G2} , then:
- (10 分) find the value of R_D .
 - (10 分) find the value of R_{G1} .
- ($\sqrt{2} = 1.414$, $\sqrt{3} = 1.732$, $\sqrt{5} = 2.24$)

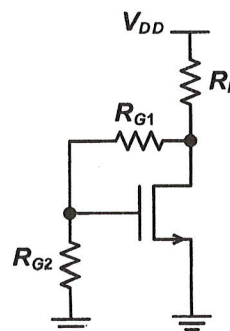


Fig. P3



4. (20 分) The transistors operate in the saturation region. $R_{D1} = R_{D2}$ and $M_1 = M_2$. $V_{in} = V_{in1} - V_{in2}$. $V_{out} = V_{out2} - V_{out1}$. (a) Calculate the differential trans-conductance? (b) Neglect the channel-length modulation and body effect of MOS transistors. Calculate the low-frequency differential small-signal voltage gain. Some related parameters are: $R_{D1,2} = 2 \text{ k}\Omega$, $\mu_n C_{ox} = 100 \times 10^{-6} \text{ A/V}^2$, $(\frac{W}{L})_{M1,M2} = 10$, and $I_{SS} = 1 \text{ mA}$.

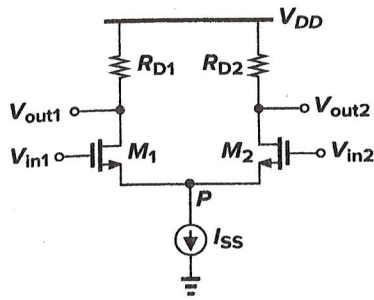


Fig. P4

5. (30 分) Both MOS transistors operate in the saturation region. Assuming neither transistor suffers from the body effect, Calculate the (a) low-frequency voltage gain of the amplifier, and (b) output resistance, and (c) 3dB bandwidth of the amplifier if $C_{out} = 20 \times 10^{-15} \text{ F}$, while ignoring the parasitic capacitances of both transistors. Some related parameter values are: $R_D = 10 \text{ k}\Omega$, $g_{m1} = 1.0 \times 10^{-3} \text{ A/V}$, $g_{m2} = 0.5 \times 10^{-3} \text{ A/V}$, $\lambda_1 = 0.1 \text{ V}^{-1}$, $\lambda_2 = 0 \text{ V}^{-1}$, and $I_{D1,2} = 1 \text{ mA}$.

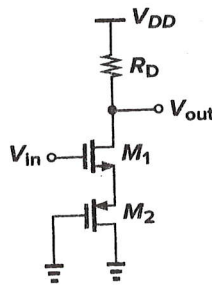


Fig. P5



Useful physical constants: $\epsilon_0 \approx \frac{10^{-9}}{36\pi}$ (F/m); $\mu_0 = 4\pi \times 10^{-7}$ (H/m)

1. (a) $\mathbf{A} = 3\mathbf{a}_x + 4\mathbf{a}_z$, $\mathbf{B} = 5\mathbf{a}_y$; (b) $\mathbf{A} = \mathbf{a}_\rho + 2\mathbf{a}_\phi + 4\mathbf{a}_z$, $\mathbf{B} = 2\mathbf{a}_\rho + 8\mathbf{a}_z$;
求 $\mathbf{A} \times \mathbf{B}$ 。(10%)
2. 電通量密度 $\mathbf{D} = 20\mathbf{a}_\rho + 10\mathbf{a}_\phi$ C/m², 請計算通過以下曲面的電通量,
曲面: $\rho = 6$ m, $0 \leq \phi \leq 90^\circ$, 與 $-1 \leq z \leq +1$ m。(10%)
3. 一個球體的電荷密度分布為 $\rho_v = \rho_a (r/a)$ 在 $0 \leq r \leq a$ 且 $\rho_v = 0$ 在 $r > a$. 請導出在所有空間 ($r > 0$) 的電通密度公式。(10%)
4. 在 $z = 1$ cm, x - y 平面無限大平板的電荷密度為 $\rho_s = +100$ nC/m², 請
計算在 $z = 0$ 位置有一接地的無限大金屬板, 其感應電荷密度。(10%)
5. 請寫出 4 個 Maxwell's eq's 以及所代表的物理意義。(10%)
6. 一個朝 $+z$ 方向傳遞的波, 其函數為 $A_0 \sin(10^8 t - \frac{1}{2} z)$, 求相速度(phase
velocity), 假設長度單位為公尺(m)。(10%)
7. 在 x - y 平面上有一無限延伸的電流平面, 其電流密度為 $\mathbf{K} = 6 \mathbf{a}_y$ A/m,
請計算 \mathbf{H} (3 m, 4 m, 5 m)。(20%)
8. 假設磁場 $\mathbf{H} = 2xy^2 \mathbf{a}_z$ A/m, 請計算電流密度 \mathbf{J} (2 m, 2 m, 3 m)。(20%)