

1.(10%)(a) In the class-A power stage of Fig. P1(a). Please derive the equation of maximum power efficiency, $\eta = \frac{P_{ac}}{P_S}$, where P_S is the power delivered by the dc power and P_{ac} is the ac power that can be delivered to the load.

(5%)(b) In the class-A power stage of Fig. P1(b). What is the function of R_E and derive the equation of maximum power efficiency again.

(15%)(c) Please describe the behavior of circuit in Fig. P1(c), and find the T_{OS} .

(Hint: Initial condition is T_2 on and T_1 off)

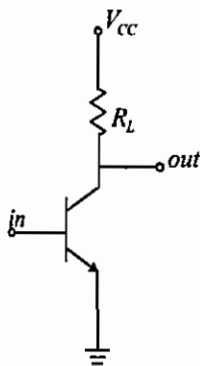


Fig. P1(a)

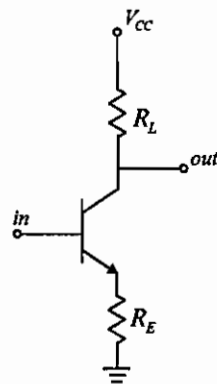


Fig. P1(b)

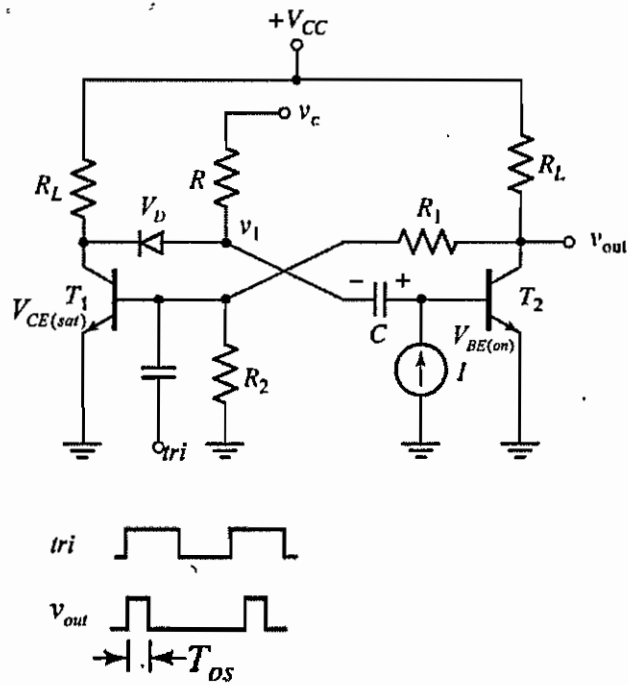


Fig. P1(c)



- 2.(10%) Consider the amplifier shown in Fig.P2, where $R_D = 1k$, $R_F = 10k$, $gm_1 = gm_2 = 0.01$, $C_A = C_X = C_Y = 100 fF$. Neglecting all other capacitances, compute the phase margin of the circuit.

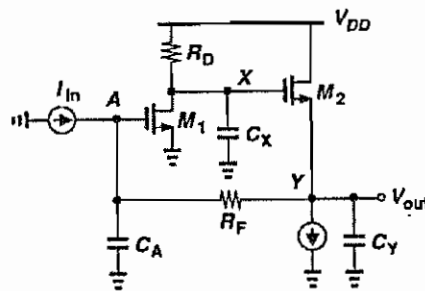


Fig. P2

- 3.(10%) Derive the transfer function of circuit shown in Fig. P3, roughly sketch its frequency response, and find the resonant frequency, ω_0 , and quality factor, Q .

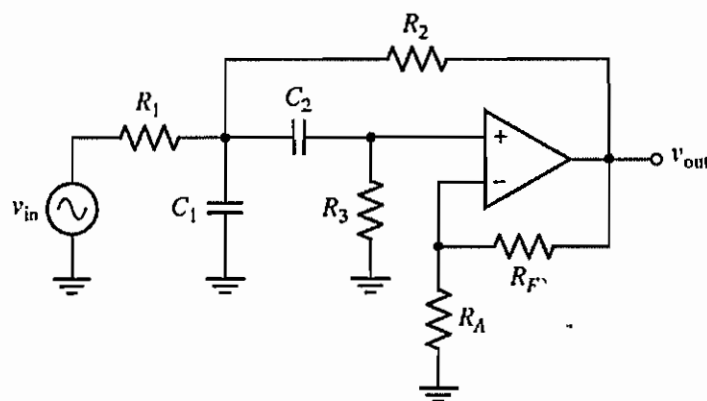


Fig. P3



4. $\mu_n C_{ox} = 60 \mu A/V^2$, $\lambda_n = 0.1 V^{-1}$, $(\frac{W}{L})_{M1} = 10$, $V_{DD} = 5V$, $R_D = 100k\Omega$, and $V_{tn} = 0.7V$. The DC or bias voltage of the input is 1V. μ is the carrier mobility. C_{ox} is the gate-oxide capacitance. λ is the channel-length modulation coefficient. $(\frac{W}{L})$ is the aspect ratio of MOSFET. V_t is the threshold voltage.

(5%) (a) Calculate g_m . (transconductance)

(5%) (b) Calculate low-frequency small-signal voltage gain.

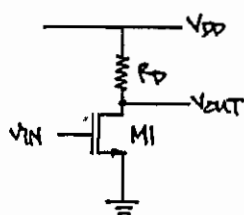


Fig. P4

5. (20%) $\mu_n C_{ox} = 60 \mu A/V^2$, $\mu_p C_{ox} = 30 \mu A/V^2$, $\lambda_n = 0.5 V^{-1}$, $\lambda_p = 0.5 V^{-1}$,

$$(\frac{W}{L})_{M1} = 100, (\frac{W}{L})_{M2} = 12, \gamma_n = 0.4 V^{1/2}, |2\phi_F| = 0.7V, V_{IN} = 4V, V_B = 1.5V, V_{DD} = 5V,$$

$R_D = 100k\Omega$, and $V_{t_{n0}} = |V_{t_{p0}}| = 0.7V$. The current source I_0 consumes a voltage

legroom of 0.5V. Please calculate the low-frequency small-signal voltage gain.

γ is the body effect coefficient of MOSFET.

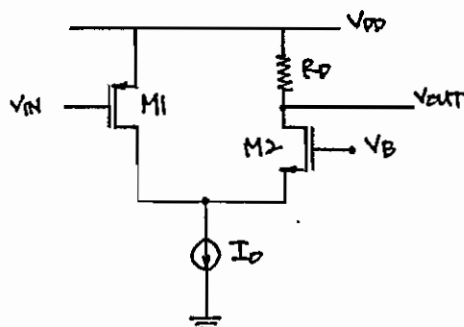


Fig. P5



6. (20%) $\mu_n C_{ox} = 60 \mu\text{A}/\text{V}^2$, $\mu_p C_{ox} = 30 \mu\text{A}/\text{V}^2$, $\lambda_n = 0\text{V}^{-1}$, $\lambda_p = 0\text{V}^{-1}$, $V_{IN} = 1.7\text{V}$,

$V_B = 3.3\text{V}$, $V_{OUT} = 3\text{V}$, $V_{DD} = 5\text{V}$, $(\frac{W}{L})_{M1} = 10$, $(\frac{W}{L})_{M2} = 2.4$, $(\frac{W}{L})_{M3} = 16$, and

$V_{m_0} = |V_{tp_0}| = 0.7\text{V}$. What is the low-frequency small-signal voltage gain of the amplifier?

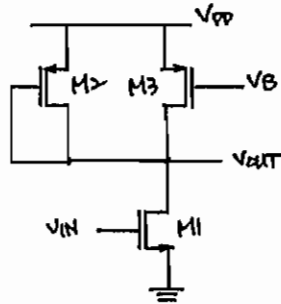


Fig. P6



本試題共 6 題，第 1 題及第 5 題每題 10 分，其餘每題 20 分，共計 100 分，請依題號作答並將答案寫在答案卷上，違者不予計分。

1. On the layout diagram Fig.1, indicate the metal connections required to create a complex CMOS logic gate implementing the function $F = \overline{AB + C + D}$. (10pt)

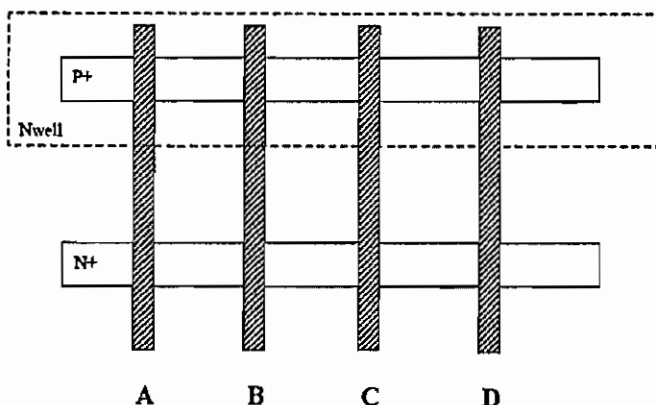


Fig. 1

2. For the following questions, choose the **best** response. (20pt)

- (I) The input to a VLSI block is 01110011. If the output is 10111001, then the block's function is: (a) Rotate Left (b) Rotate Right (c) Shift Left (d) Shift Right (e) Barrel Shift
- (II). If both a NAND gate and a NOR gate are made with ALL minimum size MOSFETs, which will have the faster rise time? (a) NAND (b) NOR (c) Same (d) Indeterminate
- (III). If both a NAND gate and a NOR gate are made with ALL minimum size MOSFETs, which will have the larger mid-point voltage for simultaneous switching? (a) NAND (b) NOR (c) Same (d) Indeterminate
- (IV) Compared to a ripple carry adder, the area of a carry look ahead adder is : (a) Larger (b) Smaller (c) Same (d) Indeterminate
- (V) If the spacing between NMOS and PMOS FETs in a output pad is decreased, the probability of latch-up will : (a) Increase (b) Decrease (c) No Change (d) Indeterminate

3. Sketch 2-input NOR gates built using: (a) clocked CMOS logic, (b) domino logic, (c) pseudo-NMOS logic, (d) CVSL logic (20pt)



4. Explain why NMOS pass **weak high** and **strong low**, and PMOS pass **weak low** and **strong high**. Use the circuits shown in Fig. 5-1 and Fig. 5-2 to help your answers.

(20pt)

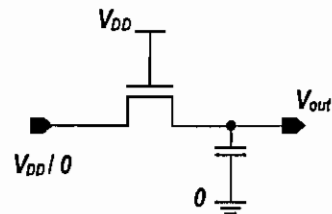


Fig. 5-1

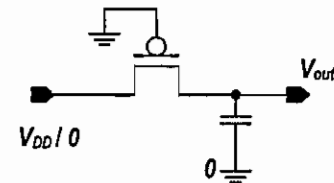


Fig. 5-2

5. Show the Boolean function of Fig. 6-1 and Fig. 6-2.

(10pt)

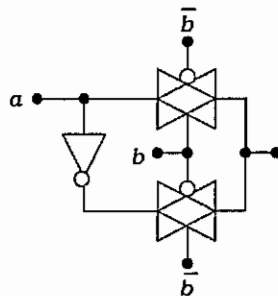


Fig. 6-1

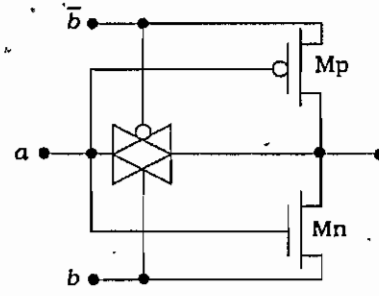


Fig. 6-2

6. Explain following terms: (a) Moore's Law, (b) SoC, (c) Body Effect, (d) LDD MOSFET. (e) DRC, ERC, LVS. (20pt)



1. If x_1, x_2, \dots, x_n are numbers, then show by induction that

$$\begin{vmatrix} 1 & x_1 & \dots & x_1^{n-1} \\ 1 & x_2 & \dots & x_2^{n-1} \\ \dots & \dots & \dots & \dots \\ 1 & x_n & \dots & x_n^{n-1} \end{vmatrix} = \prod_{i < j} (x_j - x_i),$$

the symbol on the right meaning that it is the product of all terms $x_j - x_i$ with $i < j$ and i, j integers from 1 to n . (10%)

2. Determine the sign of the following permutations. At the same time, write the inverse of the permutation. (10%)

(a) $\begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \end{bmatrix}$; (b) $\begin{bmatrix} 1 & 2 & 3 & 4 \\ 2 & 1 & 4 & 3 \end{bmatrix}$.

3. Compute the eigenvalues of the following matrix in complex numbers. (10%)

$$\begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 \end{bmatrix}$$

4. Let $X_1 = \begin{bmatrix} 1 \\ 1 \\ 0 \end{bmatrix}$, $X_2 = \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix}$, and $X_3 = \begin{bmatrix} 1 \\ 0 \\ 1 \end{bmatrix}$. Please get an orthonormal base for $\{X_1, X_2, X_3\}$. (10%)

5. Let $A = \begin{bmatrix} 1 & 4 & -2 \\ 0 & 2 & 3 \\ 4 & -1 & 1 \end{bmatrix}$. Please get the adjoint of A ($\text{adj}A$). (Note that if A is a $n \times n$ square matrix, then $A \bullet \text{adj}A = \text{adj}A \bullet A = \det A \bullet I_n$.) (10%)

6. Give 5 statements that are equivalent to a square $n \times n$ matrix being invertible. (10%)



7. Let a transformation T

$$T \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix} = \begin{bmatrix} 2x_2 - x_1 - 2x_3 \\ x_1 - x_2 \end{bmatrix}$$

- (a) (5%) Show that T is a linear transformation.
 (b) (5%) Find the transformation matrix of T with respect to the standard basis.
 (c) (10%) Find an orthonormal basis for the kernel of the matrix of T , $\ker(T)$. Give the orthogonal decomposition of the vector $[1 \ 1 \ -1]^T$ with respect to $\ker(T)$.

8. Suppose \mathbf{u} , \mathbf{v} , and \mathbf{w} are linearly independent vectors. Show that \mathbf{u} , $\mathbf{u} + \mathbf{v}$, and $\mathbf{u} + \mathbf{v} + \mathbf{w}$ are linearly independent. (10%)

9. Let T is a transformation from \mathbf{R}^2 to \mathbf{R}^2 and

$$T \left(\begin{bmatrix} x_1 \\ x_2 \end{bmatrix} \right) = \begin{bmatrix} x_1 \cos \theta - x_2 \sin \theta \\ x_1 \sin \theta + x_2 \cos \theta \end{bmatrix} = \mathbf{A}\mathbf{x}$$

- (a) (5%) Find the inverse transformation of T .
 (b) (5%) Use the inverse transformation found in (a) to solve the system given by

$$\mathbf{A}\mathbf{x} = \mathbf{b} \text{ where } \mathbf{b} = [1 \ -1]^T \text{ and } \theta = \pi.$$