



1. (10%)

Nickel has a face-centered cubic unit cell. The density of nickel is 6.84 g/cm³. Calculate a value for the atomic radius of nickel. (Ni=58.69 g/mol)

2. (10%)

An excited hydrogen atom emits light with a frequency of 1.141×10^4 Hz to reach the energy level for which $n = 4$. In what principal quantum level did the electron begin?

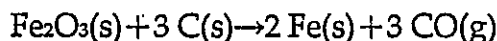
$$\text{Hint: } \Delta E = -2.178 \times 10^{-18} \left(\frac{1}{n_f^2} - \frac{1}{n_i^2} \right)$$

3. (10%)

The enthalpy of vaporization of mercury is 59.1 kJ/mol. The normal boiling point of mercury is 372°C. What is the vapor pressure of mercury at 25°C?

4. (10%)

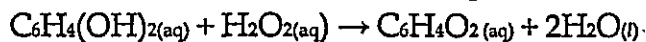
An iron ore sample contains Fe₂O₃ plus other impurities. A 652-g sample of impure iron ore is heated with excess carbon, producing 343 g of pure iron by the following reaction: (Fe=55.85)



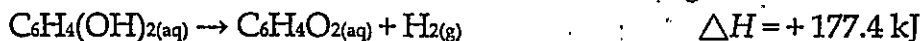
What is the mass percent of Fe₂O₃ in the impure iron ore sample? Assume that Fe₂O₃ is the only source of iron and that the reaction is 100% efficient.

5. (10%)

The bombardier beetle uses an explosive discharge as a defensive measure. The chemical reaction involved is the oxidation of hydroquinone by hydrogen peroxide to produce quinone and water:



Calculate ΔH for this reaction from the following data:





6.(10%)

A playful astronaut releases a bowling ball, of mass $m = 7.20 \text{ kg}$, into circular orbit about Earth at an altitude h of 350 km.

- What is the mechanical energy E of the ball in its orbit?
- What is the mechanical energy E_0 of the ball on the launchpad at Cape Canaveral? From there to the orbit, what is the change ΔE in the ball's mechanical energy?

7.(10%)

The cross-sectional area A_0 of the aorta (the major blood vessel emerging from the heart) of a normal resting person is 3 cm^2 , and the speed v_0 of the blood through it is 30 cm/s . A typical capillary (diameter $\approx 6 \mu\text{m}$) has a cross-sectional area A of $3 \times 10^{-7} \text{ cm}^2$ and a flow speed v of 0.05 cm/s . How many capillaries does such a person have?

8.(10%)

Figure 1. shows how the stream of water emerging from a faucet "necks down" as it falls. The indicated cross-sectional areas are $A_0 = 1.2 \text{ cm}^2$ and $A = 0.35 \text{ cm}^2$. The two levels are separated by a vertical distance $h = 45 \text{ mm}$. What is the volume flow rate from the tap?

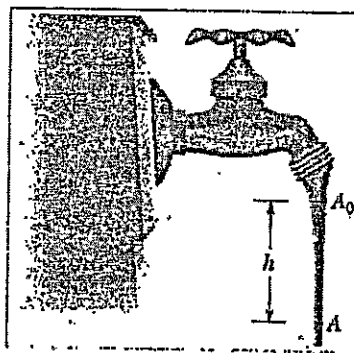


Fig. 1 . As water falls from a tap, its speed increases.

Because the flow rate must be the same at all cross sections, the stream must "neck down."



9.(10%)

A uniform solid cylindrical disk, of mass $M = 1.4$ kg, and radius $R = 8.5$ cm, rolls smoothly across a horizontal table at a speed of 15 cm/s. What is its kinetic energy K ?

10.(10%)

You are given a length of uniform heating wire made of a Nickel-chromium-iron alloy called Nichrome; it has a resistance R of 72 W. At what rate is energy dissipated in each of the following situations?
(1) A potential difference of 120 V is applied across the full length of the wire. (2) The wire is cut in half, and a potential difference of 120 V is applied across the length of each half.



國立雲林科技大學

96 學年度轉學生招生考試試題 (四年制二年級)

系別：環境與安全衛生工程系

科目：微積分

1. 試寫出 $f'(a)$ 的定義，並據此求 $f'(2)$ ，其中 $f(x) = \begin{cases} x[x], & x < 2 \\ 2x-2, & x \geq 2 \end{cases}$ (10%)
2. 試求曲線 $f(x) = \frac{x^3}{x^2-3}$ 的截距、定義域、極大及極小值、+反曲點以及漸近線並繪圖形(15%)
3. $\Omega = \left\{ (r, \theta) \mid 0 \leq r \leq 2 \cos \theta, 0 \leq \theta \leq \frac{\pi}{2} \right\}$ 求 $\iint_{\Omega} \sqrt{x^2 + y^2} d\Omega$ (15%)
4. 試求下列積分值
- (1) $\int \cos^3 x \sin^2 x dx$ (2) $\int x^2 e^x dx$ (3) $\int \frac{dx}{x^2 \sqrt{x^2 + 4}}$ (20%)
5. 求 $\frac{1}{\sqrt{(3.98)^2 + (2.99)^2}}$ 近似值 (10%)
6. Find the area of the region bounded by the parabola $y^2 = 2x - 2$ and the line $y = x - 5$. (20%)
7. Find $f'(t)$ if $f(t) = \sqrt{4 \sin^2 t + 9 \cos^2 t}$ (10%)