



1. The diffusion coefficients for copper in aluminum at 500 and 600 °C are 4.8×10^{-14} and 5.3×10^{-13} m²/s, respectively. Determine the approximate time at 500 °C that will produce the same diffusion result (in terms of concentration of Cu at some specific point in Al) as a 10-h heat treatment at 600°C. (10%)
2. Consider a single crystal of BCC iron oriented such that a tensile stress is applied along a [010] direction. Compute the resolved shear stress along a (110) plane and in a [-111] direction when a tensile stress of 52 MPa (7500 psi) is applied. (10%)
3. Using the isothermal transformation diagram for an iron-carbon alloy of eutectoid composition (Figure 1), specify the nature of the final microstructure (in terms of microconstituents present and approximate percentages) of a small specimen that has been subjected to the following time-temperature treatments. In each case assume that the specimen begins at 760 °C and that it has been held at this temperature long enough to have achieved a complete and homogeneous austenitic structure. (a) Rapidly cool to 350 °C, hold for 10^4 s, and quench to room temperature. (b) Rapidly cool to 650 °C, hold for 20 s, rapidly cool to 400 °C hold for 10^3 s, and quench to room temperature. (10%)

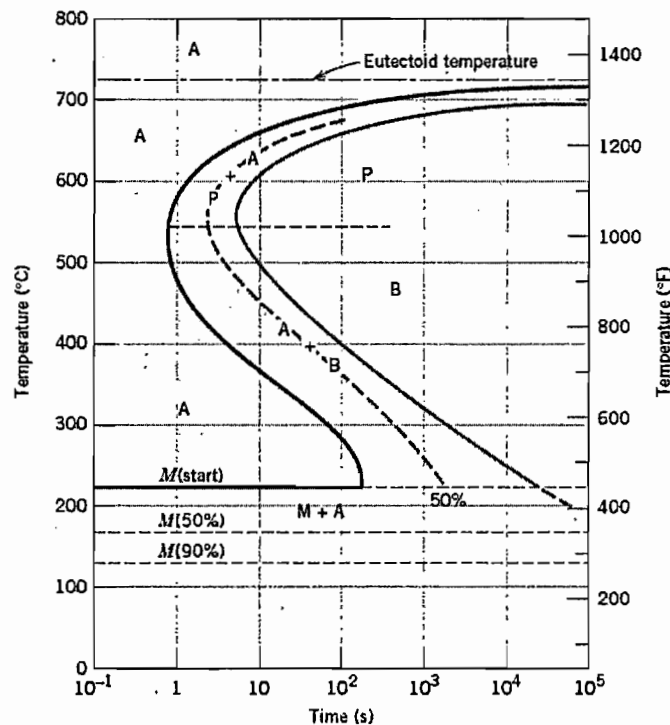


Figure 1 The complete isothermal transformation diagram for an iron-carbon alloy of eutectoid composition: A, austenite; B, bainite; M, martensite; P, pearlite.



4. On the basis of crystal structure, compute the theoretical density for sodium chloride. The sodium and chlorine ionic radii are 0.102 and 0.181 nm, respectively. $A_{\text{Na}} = 22.99 \text{ g/mol}$, $A_{\text{Cl}} = 35.45 \text{ g/mol}$. (10%)
5. Calculate the number of Schottky defects per cubic meter in potassium chloride at 500 °C. The energy required to form each Schottky defect is 2.6 eV, while the density for KCl (at 500 °C) is 1.955 g/cm^3 . $A_{\text{K}} = 39.10 \text{ g/mol}$, $A_{\text{Cl}} = 35.45 \text{ g/mol}$, Boltzmann's constant is $1.3806504 \times 10^{-23} \text{ J/K}$. (10%).
6. A high-molecular-weight polyethylene has an average molecular weight of 410,000 g/mol. What is its average degree of polymerization? (10%).
7. Define the following phases that exist in the Fe-Fe₃C phase diagram: (a) austenite, (b) α ferrite, (c) cementite, (d) δ ferrite. (10%).
8. In the solidification of a pure metal, what are the two energies involved in the transformation? Write the equation for the total free-energy change involved in the transformation of liquid to produce a strain-free solid nucleus by homogeneous nucleation. Find the critical size to form a stable nucleus. (10%).
9. According to electron energy band structure, explain electrical conductivities of metals, semiconductors, and insulators. (10%).
10. A plain-carbon steel contains 93 wt % ferrite and 7 wt % Fe₃C. What is its average carbon content in weight percent? (10%).



注意：每題答案 10 分，共 10 題。

- 1) IF $f(x) = x^3 - 26, x \in [2,3]$, SHOW THAT THE FUNCTION f HAS ONLY ONE ZERO (零位) IN THE INTERVAL $[2,3]$.
- 2) APPROXIMATE $\sqrt[3]{26}$ BY
 - a) DIFFERENTIAL METHOD,
 - b) NEWTON METHOD: FIND THE NEXT SOLUTION IF THE INITIAL SOLUTION 3 IS GIVEN.
- 3) SOLVE $\frac{dW}{dt} = kW(t)$, WITH $W(0) = M$ AND $k < 0$.; THEN FIND THE HALF-LIFE (半衰期).
- 4) a) GIVE THE DEFINITION OF THE DIRECTIONAL DERIVATIVE (方向導數) OF $Z = F(X, Y)$ AT THE POINT (a, b) WITH THE DIRECTION VECTOR $U = (\alpha, \beta)$.
b) FIND THE DIRECTION OF MAXIMUM INCREASE OF F .
- 5) IF $E = \{(x, y) \mid \frac{x^2}{9} + \frac{y^2}{16} \leq 1\}$, FIND THE AREA OF E .
6. If $\lim_{x \rightarrow 0} \left(\frac{\sin 2x}{x} + \frac{1 - \cos x}{x} + \frac{1 - \cos x}{x^2} \right) = a$, find a .
7. Find $\int_0^{\pi/2} \sin 2\theta \, d\theta$.
8. Is $\sum_{n=2}^{\infty} \frac{1}{n \ln n}$ convergent?
9. Find the Maclaurin series for $\ln(1+x)$.
10. Find the relative extrema of $f(x) = x^3 + y^3 + 3xy + 3$.