



1. (10%) Solve the differential equation: $\frac{dy}{dx} + xy = \frac{2x}{y}$.
2. (10%) Solve the differential equation: $y'' - 5y' + 6y = 4 \sin 4x$.
3. (15%) Find the eigenvalues and eigenvectors of the matrix: $\begin{bmatrix} 2 & 0 & 1 \\ -1 & 4 & -1 \\ -1 & 2 & 0 \end{bmatrix}$.
4. (15%) Find the Fourier series for the periodic function defined by $f(t) = \frac{2}{\pi}t + 2$ for $-\pi \leq t \leq \pi$, and $f(t+2\pi) = f(t)$.
5. (10%) Please use the separation of variables to find the solution of the partial differential equation $y \frac{\partial^2 u}{\partial x \partial y} + u = 0$.
6. (15%) Please solve the wave equation $a^2 \frac{\partial^2 u}{\partial x^2} = \frac{\partial^2 u}{\partial t^2}$, $0 < x < L, t > 0$, subject to $u(0,t) = 0$, $u(\pi,t) = 0$, $u(x,0) = 0$, $\frac{\partial u}{\partial t} \Big|_{t=0} = \sin x$.
7. (10%) Please solve (1) $\ln(3-2i)$, (2) $\sin(2i)$.
8. (15%) Please solve the integral value of $\oint_C \frac{\cos \pi z}{(z-1)^5} dz$, where the contour C is the circle: $|z| = r > 1$.



1. Explain or define the following terms:
 - (a) Ionization energy of donor impurities in a semiconductor (5%)
 - (b) Built-in potential of p-n junction (5%)
 - (c) Fermi-Dirac distribution of electrons in a semiconductor (5%)
 - (d) Effective mass of holes (5%)
2. Make a comparison between the abrupt and the graded p-n junctions. (15%)
3. Describe the basic electrical properties of a Schottky-barrier junction. (15%)
4. Selection problem set: (15%)
 - (1) The turn-on voltage of an Al-Si Schottky diode may be
(A) 0.05V (B) 0.35V (C) 0.75V (D) 2.5V .
 - (2) When the temperature is increased from 50°K to 200°K, the conductance of a doped semiconductor is
(A) increased (B) decreased (C) unchanged (D) undecided
 - (3) Mobility of carrier is not dependent on
(A) temperature (B) doping concentration (C) electrical field (D) defect
 - (4) What semiconductor parameter can't be obtained by Hall measurement?
(A) conductive type (B) minority carrier mobility
(C) minority carrier concentration (D) majority carrier mobility
 - (5) What may decrease when temperature is increased?
(A) intrinsic concentration (B) mobility
(C) Fermi-Dirac distribution function (D) energy band gap
5. A set of parameters of silicon npn common-emitter BJT are given as $N_B = 5 \times 10^{16}$, $N_E = 5 \times 10^{18}$, $N_C = 5 \times 10^{15}$, $\mu_E = 250$, $\mu_B = 1000$, $\tau_{B0} = 5 \times 10^{-7}$ s, $x_B = 0.25 \mu\text{m}$, x_C and x_E are long.
 - (a) V_{BE} is hold constant voltage about 0.6V. If V_{BC} is changed from 0V to 10V, find the changed percentage of I_C ? (10%)
 - (b) I_B is hold constant under $V_{BE} = 0.6\text{V}$ and $V_{BC} = 0\text{V}$. If V_{BC} is changed from 0V to 10V, find the changed percentage of I_C ? (10%)
6. Explain (a) flat band voltage, (b) short channel effect and (c) Zener breakdown. (15%)

$$[n_i = 1.5 \times 10^{10}, V_t = 26\text{mV}, \epsilon_s = 11.7\epsilon_0, \epsilon_0 = 8.85 \times 10^{-14}, \phi_m(\text{Al}) = 4.28\text{V}]$$



1. A spherical distribution of charge $\rho = \rho_0 [1 - (R^2/b^2)]$ exists in the region $0 \leq R \leq b$. This charge distribution is concentrically surrounded by a conducting shell with inner radius $R_i (> b)$ and outer radius R_o . Determine \mathbf{E} everywhere (10%) and the surface charge density at the inner and outer surfaces of the conductor. (10%)
2. Two infinitely long coaxial cylindrical surfaces, $r = a$ and $r = b$ ($b > a$), carry surface charge densities ρ_{sa} and ρ_{sb} , respectively. Determine \mathbf{E} everywhere. (15%)
3. Two blocks of conducting materials are in contact at the $y = 0$ plane. At a point P in the interface, the current density is $\mathbf{J}_1 = 10 (\mathbf{a}_y 4 + \mathbf{a}_z 3)$ (A/m²) in medium 1 (conductivity σ_1). Determine \mathbf{J}_2 at P in medium 2 if $\sigma_2 = 2\sigma_1$. (15%)
4. Assume the xy -plane is the interface between two media. If the magnetic field intensity \mathbf{H}_1 in medium 1 (permeability μ_1) is $-3\mathbf{a}_x - 4\mathbf{a}_z$ (A/m) at the interface, find the magnetic field intensity \mathbf{H}_2 in medium 2 (permeability μ_2). Assume that $\mu_1 = 2\mu_2$, and the surface current density at the interface $= -\mathbf{a}_y 2$ A/m. (15%)
5. Determine the magnetic force per unit length between two infinitely long, thin, parallel conducting wires carrying I_1 and I_2 in the same direction. The wires are separated by a distance d . (10%)
Also determine the direction of the force (attraction or repulsion). (5%)
6. The instantaneous expression for the magnetic field intensity of a uniform plane wave propagating in the $+y$ direction in air is given by

$$\mathbf{H} = \mathbf{a}_z 4 \times 10^{-6} \cos(2 \times 10^7 \pi t - k_0 y + \frac{\pi}{4}) \quad (\text{A/m})$$
 - (a) Determine k_0 . (10%)
 - (b) Write the instantaneous expression for \mathbf{E} . (10%)