



1. Assuming that the diodes in the circuit of Figure 1 are ideal, find and sketch the transfer characteristic v_o versus v_i . (20%)

2. For the circuit in Figure 2, assuming all transistors to be identical with β infinite. (30%)
 - (a) Derive an expression for the output I_o , and show that by selecting $R_1 = R_2$ and keeping the current in each junction the same, the current I_o will be

$$I_o = \frac{\alpha V_{CC}}{2R_E}$$
 - (b) What must the relationship of R_E to R_1 and R_2 be?
 - (c) For $V_{CC} = 15$ V, and assuming $\alpha \cong 1$ and $V_{BE} = 0.7$ V, design the circuit to obtain an output current of 1 mA. What is the lowest voltage that can be applied to the collector of Q_3 ?

3. The differential amplifier circuit of Figure 3 utilizes a resistor connected to the negative power supply to establish the bias current I . (30%)
 - (a) For $v_{B1} = v_d/2$ and $v_{B2} = -v_d/2$, where v_d is a small signal with zero average, find the magnitude of the differential gain, $|v_o/v_d|$.
 - (b) For $v_{B1} = v_{B2} = v_{CM}$, find the magnitude of the common-mode gain, $|v_o/v_{CM}|$.
 - (c) If $v_{B1} = 0.1 \sin 2\pi \times 60t + 0.005 \sin 2\pi \times 500t$ volts,
 $v_{B2} = 0.1 \sin 2\pi \times 60t - 0.005 \sin 2\pi \times 500t$ volts, find v_o .

4. The BJTs (bipolar-junction transistors) in the Darlington follower of Figure 4 having $\beta_o = 100$. If the follower is fed with a source having a $100 \text{ k}\Omega$ resistance and is loaded with $1 \text{ k}\Omega$, find the input resistance and the output resistance (excluding the load) and the overall voltage gain (both open circuited and with load). (20%)

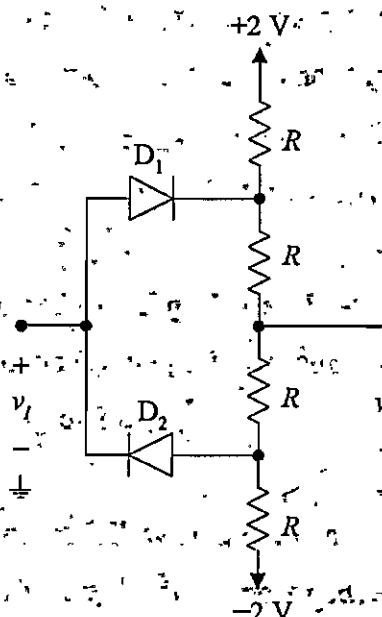


Figure 1

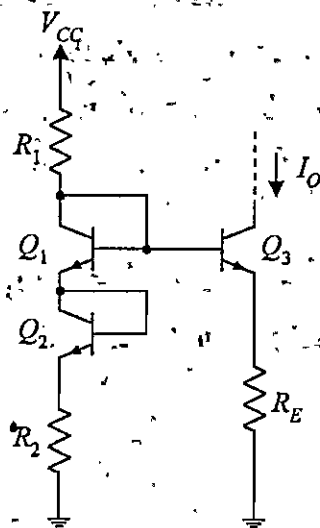


Figure 2

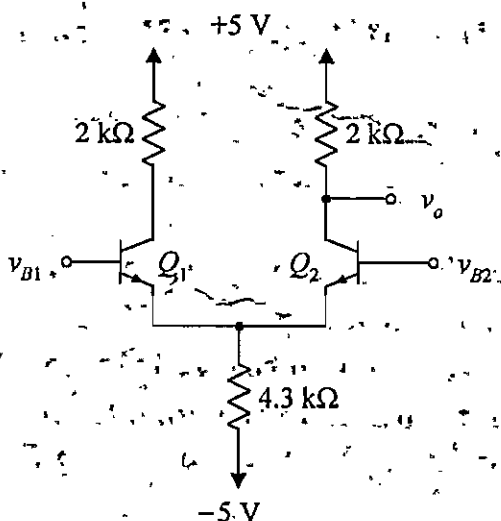


Figure 3

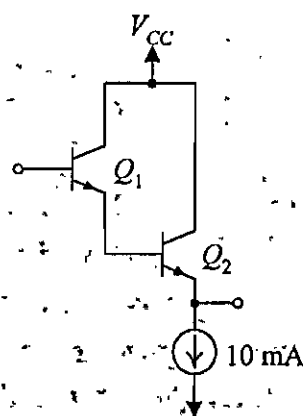


Figure 4



- Label the following statements as being true or false. (18%)
 - The rank of a matrix is equal to the number of its nonzero columns.
 - If S generates the vector space V , then every vector in V can be written as a linear combination of elements of S in only one way.
 - Any system of n linear equations in n unknowns has at least one solution.
 - The matrices $A, B \in M_{n \times n}(F)$ are called similar if $B = Q^{-1}AQ$ for some $Q \in M_{n \times n}(F)$.
 - If Q is an invertible matrix, then $\det(Q^{-1}) = [\det(Q)]^{-1}$.
 - If B is a matrix obtained from A by interchanging two rows, then $\det(B) = -\det(A)$.

- Solve the linear equations using Gaussian elimination (16%)

$$\begin{cases} 2x_1 - 2x_2 - x_3 + 6x_4 - 2x_5 = 1 \\ x_1 - x_2 + x_3 + 2x_4 - x_5 = 1 \\ 4x_1 - 4x_2 + 5x_3 + 7x_4 - x_5 = 1 \end{cases}$$

- Compute $\lim_{m \rightarrow \infty} A^m$ for the following matrices A . (16%)

$$(i) \begin{pmatrix} -1.8 & 0 & -1.4 \\ -5.6 & 1 & -2.8 \\ 2.8 & 0 & 2.4 \end{pmatrix} \quad (ii) \begin{bmatrix} -2 & -1 \\ 4 & 3 \end{bmatrix}$$

- Determine the frequency of oscillation of the pendulum of length L in Fig. A. Neglect air resistance and the weight of the rod. Assume that θ is small enough. (10%)

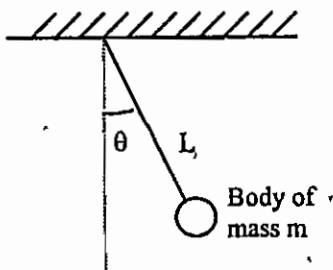


Fig. A



5. Given the equation $xy'' + 2y' + xy = 0$, if $y_1 = \frac{\sin x}{x}$ is a solution of the given equation. Find another linearly independent solution y_2 . (10%)

6. Find the general solution of the following equation:

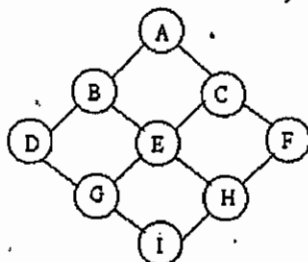
(a) $y'' - 2y' + y = \frac{e^x}{x^3}$ (10%)

(b) $x^2 y'' - xy' = 2x^3 e^x$ (10%)

(c) $y'' + 4y = 8xe^{-2x} + 4x^2 + 2$ (10%)



- 10 points 1. Simulate the function SelectionSort on an array containing the elements 25, 34, 14, 16, 29, 30. How many **comparisons** and **swaps** of elements are made?
- 10 points 2. Let array A[-1:3,2:5,-1:4,-2:2] store data by row-major order. If the starting address of array A is 100 and each element of array A requires 2 memory unit, compute the address of A[3,4,3,0].
- 10 points 3. For each of the expressions
 a) $((x-y)*z+(y-w))*x$
 b) $((((a*x+b)*x+c)*x+d)*x+e)*x+f$
 do the followings:
 a) Find the equivalent prefix expression. (5 points)
 b) Find the equivalent postfix expression. (5 points)
- 10 points 4. Apply heapsort to the list of elements 3, 1, 4, 1, 5, 9, 2, 6, 5. First give the intermediate results after heapifying the array, and then sort the array step by step.
- 10 points 5. For the following graph, construct the depth-first search tree and breadth-first search tree from node A, respectively.



- 10 points 6. Consider the following C program segment, where i , j , and k are integer variables.

```

for (i = 1; i <= 10; i++)
  for (j = 1; j <= i; j++)
    for (k = 1; k <= j; k++)
      printf ("%d\n", i*i+j-k);

```

How many times is the *printf* statement executed in this program segment?

- 10 points 7. Suppose that the C language does not provide the assignment operator =. Write a function that perform the assignment operation. This function's prototype has this form:

```

/* assign q to p, i.e. p = q */
void assignment(int *p, int q)

```

We assume that q is a positive integer variable. You can use any C instructions or operators except the assignment operator to complete this question. (Hint: the C language provides the increment operator ++ and the decrement operator --.)



國立雲林科技大學

八十七學年度研究所碩士班入學考試試題

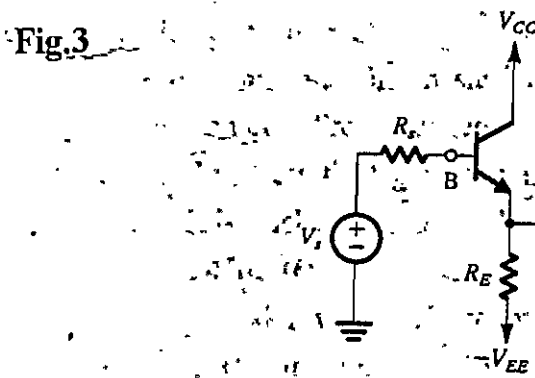
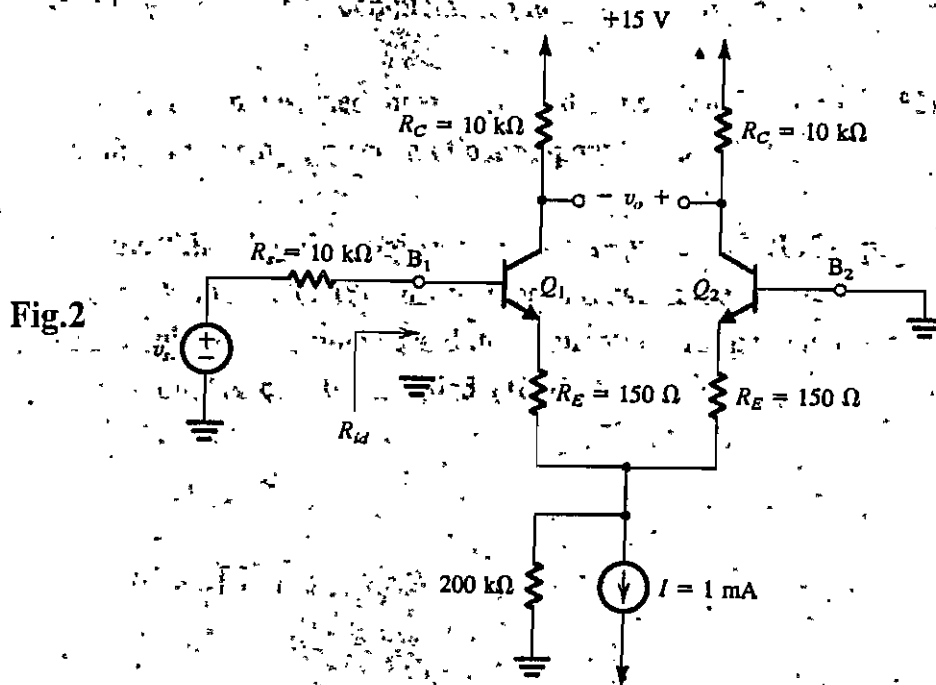
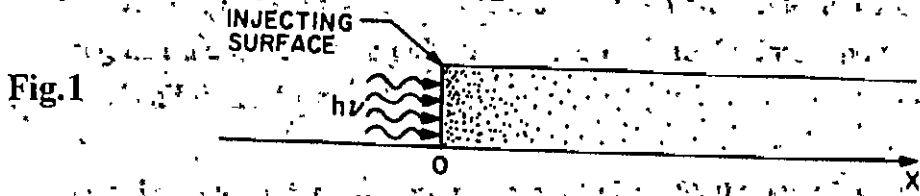
所別：電子所

科目：計算機概論 (乙)

- 10 points 8. Describe the concept of the John von Neumann Machines.
- 10 points 9. From the list: 2, 5, 7, 10, 24, 32, extract a collection of numbers where sum is 41. What is the complexity of your method for solving this problem? Does this appear to be a polynomial problem or a nonpolynomial problem?
- 10 points 10. Identify three software utilities that normally accompany an operating system.



1. Determine the electron and hole concentrations in a silicon sample at room temperature containing 2.0×10^{17} phosphorus atoms/cm³ and 8.0×10^{15} boron atoms/cm³. (15%)
2. Describe briefly the fabrication process sequence of a silicon enhancement-mode N-channel MOSFET using the planar IC technology. (15%)
3. Sketch the circuit diagram of a CMOS inverter and explain its operation. (20%)
4. Figure 1 shows that a p-type Si semiconductor (with $10^{17}/\text{cm}^3$, $\mu_p=300$ and $\mu_n=800 \text{ cm}^2/\text{V-s}$) where the electron-hole pairs are created from one side as a result of incoming photon flux (10^{14} photons/s-cm² and $h\nu \gg E_g$). Find the total current at the surface. (10%)
5. The differential amplifier in Fig.2 uses transistors with $\beta=100$. Evaluate the following: (1) The input differential resistance R_{id} . (2) The overall voltage gain v_o/v_s (neglect the effect of r_o). (3) The worst-case common-mode gain if the two collector resistors are accurate to within $\pm 1\%$. (4) The CMRR, in dB. (5) The input common-mode resistance (assuming that the Early voltage $V_A=100 \text{ V}$ and that $r_{\mu}=10 \beta r_o$). (25%)
6. For an emitter follower, as shown in Fig.3, biased at $I_C=1\text{mA}$ and having $R_s = R_E = 1\text{k}\Omega$, and using a transistor specified to have $f_T = 400\text{MHz}$, $C_{\mu}=2\text{pF}$, $r_x=100$, and $\beta_o=100$, evaluate the midband-gain A_M and the frequency of the dominant high-frequency pole. (15%)





1. A string of address references given as byte addresses is listed as follows: 1, 5, 8, 3, 40, 17, 19, 56, 49, 11, 14, 43, 20, 48, 79, 107. Consider a two-way set associative cache with a total of 8 lines and the line size is 4 bytes. Label each reference in the list as a hit or miss and show the final contents of the cache. Assuming that the lines are initially empty, the LRU replacement policy is used, and way 0 is allocated first. (10%)

2. What does the following bit pattern represent? 1100 0000 0000 0000 0000 0000 0000 0000
 - a. Assuming it is a two's complement integer? (give the answer in hex form) (3%)
 - b. Assuming it is an unsigned integer? (give the answer in hex form) (3%)
 - c. Assuming it is a single precision floating-point number? (4%)

3. Translate the following C expressions into a sequence of RISC-type assembly instructions. Define each RISC instructions you use in the register transfer form. Each line should have comments and the assumptions for passing the parameters in registers should be clearly identified. (10%)

```
While (A[i] == j)
{
    i++;
    A[i] = A[i] - j;
}
```

4. Design the memory system for a microprocessor. The processor uses 32-bit logical address and 32-bit external data bus.
 - a). Show the design of a direct-mapped TLB. This TLB has 16 entries. The page size is 4KB. Assuming that the physical address is also 32-bit long. (6%)
 - b). Show the design of a direct-mapped cache of 8KB. The line size is 32 bytes. It uses physical address for tags. Show the relationship of this cache with the TLB above. This cache uses the MESI protocol. Assuming the cacheable memory area is 4GB. (6%)
 - c). Show the design of a two-way interleaving DRAM main memory system for this processor. The memory size is 512MB using 16Mx4 DRAM chips. Assuming this memory is located at the lowest address space. The processor uses little endian mode. (8%)



5. Use an one-pass assembler described by Beck to assemble the following SIC program.
- List the symbol table content after the assembler has processed line 4. (5%)
 - List the symbol table content after the assembler has processed line 9. (5%)
 - List the symbol table content after the assembler has processed line 12. (5%)

Line

1 SUM START 4000

2 FIRST LDX ZERO

3 LDA ZERO

4 LOOP ADD T1,X

5 TIX CNT

6 JLT LOOP

7 STA TAL

8 RSUB C

9 T1 RESW 2

10 CNT RESB 1

11 ZERO WORD 0

12 TAL RESW 1

13 END FIRST

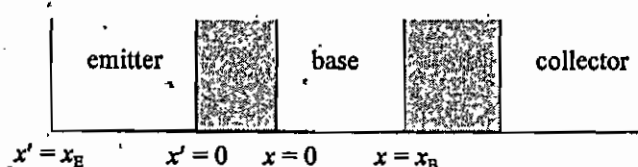
6. By using two semaphores initially set $S_1=3$ and $S_2=0$, how can you synchronize two processes, one (producer) filling a buffer and the other (consumer) emptying it? It is assumed that the system has three buffers. (15%)
7. Describe the differences between Unix swapping systems and Unix demand paging systems. (10%)
8. Compare and contrast the Window95 terms: "DLL", "OLE" and "DDE". (10%)



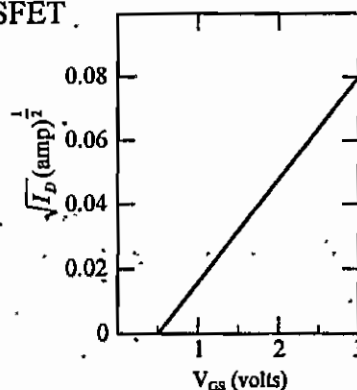
- Starting with the continuity equations for electrons and holes, please derive the Ambipolar transport equation. (20%)
- Please describe in details the two major physical mechanisms giving rise to the reversed-bias breakdown in a p-n junction semiconductors. (15%)
- Assume that the donor concentration in an n-type semiconductor at $T = 300$ K is given by

$$N_d = 10^{16} - 10^{19} x$$
 where x is given in cm and ranges between 0 and 1 μm .
Please determine the induced electric field in a semiconductor in thermal equilibrium. (15%)
- Consider a contact between Al and n-Si doped at $N_d = 10^{16} \text{ cm}^{-3}$.
 - Draw the ideal energy band diagram at zero bias after the junction is formed. (5%)
 - Determine the theoretical barrier height ϕ_{B0} and the built-in potential barrier V_{bi} . (5%)
 - Another type of metal is used to form an ohmic contact with the same n-Si. Draw the ideal energy-band diagram with a positive voltage applied to the metal. (5%)
 Al work function: 4.28 volts. $T = 300$ K.
- The following currents are measured in a uniformly doped npn bipolar transistor:

$$\begin{aligned} J_{nE} &= 1.20 \times 10^3 \text{ A/cm}^2 && \text{(due to the electron diffusion at } x = 0) \\ J_{nC} &= 1.19 \times 10^3 \text{ A/cm}^2 && \text{(due to the electron diffusion at } x = x_B) \\ J_{pE} &= 0.02 \times 10^3 \text{ A/cm}^2 && \text{(due to the hole diffusion at } x' = 0) \\ J_R &= 0.05 \times 10^3 \text{ A/cm}^2 && \text{(due to the recombination in the forward-biased B-E junction)} \end{aligned}$$



- Determine the ratio of emitter doping to base doping in order to achieve this result. Assuming $x_B \ll L_B$ and $x_E \ll L_E$, $x_B = x_E$, and $D_E = D_B$. (5%)
 - Determine the small-signal common base current gain α and common emitter current gain β . (10%)
 - If the base width x_B is reduced by 50%, what is the new value of α ? (5%)
- The experimental characteristics of an ideal n-channel MOSFET biased in the saturation region are shown in the figure.
 - If $W = 20 \mu\text{m}$ and $L = 2 \mu\text{m}$, and $t_{ox} = 100 \text{ \AA}$, determine the threshold voltage and the inversion carrier mobility. (10%)
 - If the source bias is zero and the substrate bias is changed from zero to negative, how does the threshold voltage change? Explain. (5%)





Silicon, gallium arsenide, and germanium properties ($T = 300^{\circ}\text{K}$)

Property	Si	GaAs	Ge
Atoms (cm^{-3})	5.0×10^{22}	4.42×10^{22}	4.42×10^{22}
Atomic weight	28.09	144.63	72.60
Crystal structure	Diamond	Zincblende	Diamond
Density (g/cm^{-3})	2.33	5.32	5.33
Lattice constant (\AA)	3.57	3.57	3.57
Melting point ($^{\circ}\text{C}$)	1415	1238	937
Dielectric constant	11.7	13.1	16.0
Bandgap energy (eV)	1.12	1.42	0.66
Electron affinity, χ , (volts)	4.01	4.07	4.13
Effective density of states in conduction band, N_c , (cm^{-3})	2.8×10^{19}	4.7×10^{17}	1.04×10^{19}
Effective density of states in valence band, N_v , (cm^{-3})	1.04×10^{19}	7.0×10^{18}	6.0×10^{18}
Intrinsic carrier concentration (cm^{-3})	1.5×10^{10}	1.8×10^6	2.4×10^5
Mobility ($\text{cm}^2/\text{V}\cdot\text{s}$)			
Electron, μ_n	1350	8500	3900
Hole, μ_p	480	400	1900
Effective mass, $(\frac{m^*}{m_0})$			
Electrons	$m_e^* = 0.98$ $m_h^* = 0.19$	0.067	1.64
Holes	$m_e^* = 0.16$ $m_h^* = 0.49$	0.082	0.082
Effective mass (density of states)			
Electrons, $(\frac{m^*}{m_0})$	1.08	0.067	0.55
Holes, $(\frac{m^*}{m_0})$	0.56	0.48	0.37

Physical constants

Avogadro's number	$N_A = 6.02 \times 10^{23}$
Boltzmann's constant	$k = 1.38 \times 10^{-23} \text{ J/K}$ $= 8.62 \times 10^{-5} \text{ eV/K}$
Electronic charge (magnitude)	$e = 1.60 \times 10^{-19} \text{ C}$
Free electron rest mass	$m_0 = 9.11 \times 10^{-31} \text{ kg}$
Permeability of free space	$\mu_0 = 4\pi \times 10^{-7} \text{ H/m}$
Permittivity of free space	$\epsilon_0 = 8.85 \times 10^{-14} \text{ F/cm}$ $= 8.85 \times 10^{-12} \text{ F/m}$
Planck's constant	$h = 6.625 \times 10^{-34} \text{ J}\cdot\text{s}$ $= 4.135 \times 10^{-15} \text{ eV}\cdot\text{s}$
Proton rest mass	$M = 1.67 \times 10^{-27} \text{ kg}$
Speed of light in vacuum	$c = 2.998 \times 10^{10} \text{ cm/s}$
Thermal voltage ($T = 300^{\circ}\text{K}$)	$V_T = \frac{kT}{e} = 0.0259 \text{ volt}$ $kT = 0.0259 \text{ eV}$

Properties of SiO_2 and Si_3N_4 ($T = 300^{\circ}\text{K}$)

Property	SiO_2	Si_3N_4
Crystal structure	[Amorphous for most integrated circuit applications]	
Atomic or molecular density (cm^{-3})	2.2×10^{22}	1.48×10^{22}
Density ($\text{g}\cdot\text{cm}^{-3}$)	2.2	3.4
Energy gap	$\approx 9 \text{ eV}$	4.7 eV
Dielectric constant	3.9	7.5
Melting point ($^{\circ}\text{C}$)	≈ 1700	≈ 1900



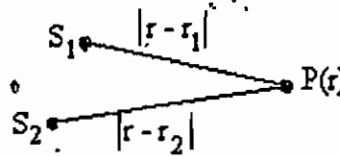
本試卷共有六大題，總分 100 分。

- 一、試設計一實驗步驟以量測多模光纖的數值孔徑(numerical aperture; N.A.)，並說明其學理？ (20 分)

- 二、設有二同一波長之單色光源 S_1 及 S_2 ，其發出的光波到達 P 點時，其電場分別為(參考圖一)

$$E_1 = E_{10} \sin(kr_1 - \omega t)$$

$$E_2 = E_{20} \sin(kr_2 - \omega t + \delta)$$



其中 k 為波數， ω 為角頻率， δ 為光源 S_1 與 S_2 間的相角差，可能為時間的函數 $\delta(t)$ 。已知光強度 I 正比於電場之平方值 E^2 ，試求於 P 點量測出的光波平均總強度？ (15 分)

- 三、試以三能階系統說明紅寶石雷射操作之基本原理，並以圖示解釋之？ (15 分)

- 四、已知以波長 1849 埃(A)紫外光照射於鉬金屬板上，量測得到光電子的阻尼電位(retarding potential) 為 2.72 伏特(V)，試計算鉬金屬之低限頻率(threshold frequency)及功函數(work function)？ (已知蒲朗克常數為 6.625×10^{-34} 焦耳·秒) (15 分)

- 五、試說明如何利用光吸收的實驗結果，以求得直接(direct)半導體之能隙(energy gap)，並以圖示解釋之？ (15 分)

- 六、解釋名詞 (20 分)

- (a) 量子效率(quantum efficiency) (5 分)
 (b) 布魯斯特角 (Brewster angle) (5 分)
 (c) 黑體輻射(black body radiation) (5 分)
 (d) 全反射(total reflection) (5 分)



1. (15%)

For the zero-order-hold sampling scheme, sampling is done by sampling at nT_s and holding the result until the time of the next sample $(n+1)T_s$. Derive the relation between $X_s(f)$ and $X(f)$ which are the Fourier transform of the sampled signal $x_s(t)$ and the original signal $x(t)$, respectively.

2. (10%)

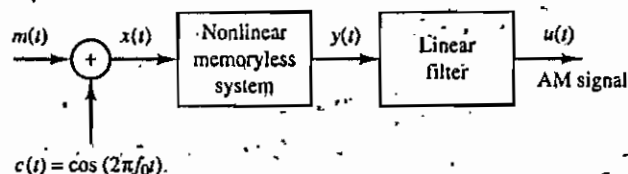
Find the value of

$$\int_{-\infty}^{\infty} \text{sinc}^3(t) dt$$

3. (15%)

The system shown in the following figure is used to generate an AM signal. The modulating signal $m(t)$ has zero mean and its maximum (absolute) value is $A_m = \max|m(t)|$. The nonlinear device has an input-output characteristic

$$y(t) = ax(t) + bx^2(t)$$



- Express $y(t)$ in terms of the modulating signal $m(t)$ and the carrier $c(t) = \cos(2\pi f_c t)$.
- Specify the filter characteristics that yield an AM signal at its output.
- What is the modulation index?

4. (15%) Consider a lowpass signal $m(t)$ with the Fourier transform

$$M(f) = \begin{cases} 2 - |f|, & |f| < 2 \\ 0, & |f| \geq 2 \end{cases}$$

We construct a bandpass signal $x(t) = 6m(t)\cos(2\pi f_0 t) + 6\hat{m}(t)\sin(2\pi f_0 t)$, where $f_0 > 2$ and $\hat{m}(t)$ is the Hilbert transform of $m(t)$.

- Find $m(t)$.
- Find the lowpass equivalent signal of $x(t)$.
- Sketch the Fourier transform of $x(t)$.



5. (10%) In an analog communication system, the demodulation gain, G , is defined as the ratio of the SNR at the output of the demodulator to the SNR at the output of the noise-limiting filter at the receiver front end. Find the demodulation gain in each of the following cases.

- (a) SSB (single sideband).
- (b) FM with modulation index β_f .

6. (15%) A source has an alphabet $\{a, b, c, d\}$ with corresponding probabilities $\{\frac{1}{2}, \frac{1}{4}, \frac{1}{8}, \frac{1}{8}\}$.

- (a) Find the entropy of the source (in bits/symbol).
- (b) Design a Huffman code for the source.
- (c) What is the average length of the Huffman code?

7. (20%) Consider an M-ary modulator with $M=5$ signals

$$s_m(t) = \begin{cases} \cos(\omega_0 t - \frac{m}{2}\pi); & m = 0, 1, 2, 3 \\ 0; & m = 4 \end{cases}$$

$$0 \leq t \leq T, \quad \omega_0 T = 100\pi.$$

- (a) Find the orthonormal basis functions.
- (b) Find the signal constellation.
- (c) Sketch the decision regions.
- (d) Sketch the optimum receiver for an AWGN channel, using $s_m(t)$, $m = 0, 1, 2, 3, 4$, as the reference signals.



1. (20pts) Assume that A and B are two 4-bit unsigned integers. Please
- design a 4×4 bit multiplier based on the 2×2 bit multipliers. (5pts) (Note: you can use a black box to represent a 2×2 bit multiplier and include other components if necessary)
 - design a 4×4 bit multiplier if only full adders and AND gates are available in your design, i.e., to implement an 4×4 bit array multiplier for unsigned numbers. (5pts)
 - show the critical path in (b) and find the worst-case execution time of your design. (5pts)
 - compare the performance of radix-2 and radix-4 implementation. (5pts)

2. (20pts) For the following three 4-input functions

$$f_1(a, b, c, d) = \Sigma (0, 1, 2, 7, 8, 9)$$

$$f_2(a, b, c, d) = \Sigma (0, 2, 6, 7, 8, 9, 10, 13, 15)$$

$$f_3(a, b, c, d) = \Sigma (0, 2, 6, 7, 8, 10)$$

- please use the tabular (Quine-McCluskey) method to minimize the two-level sum-of-product expression of the function f_2 . (10pts)
- derive a two-level all-NAND circuit that realizes f_1 , f_2 , and f_3 with the minimum cost. (10pts) (Note: You can use either K-maps or the tabular method for the multiple-output realization)

3. (20pts) For an expression tree as shown in Figure 1.

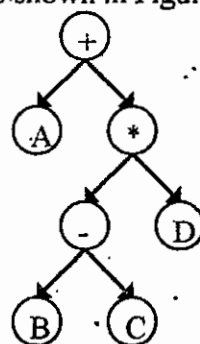


Figure 1

Using C (or whatever language you are familiar with), please

- define the data structure of a tree node (6pts)
- write down the prefix, infix and postfix expressions (7pts)
- code a function "prefix(root_of_tree)" which can traverse the tree and print out its prefix expression (7pts)